

TESLA EV 1.5 PERFORMANCE SIMULATION

http://www.leapcad.com/Transportation/Tesla_Simulation.mcd

VXPhysics.com

Tesla - Vehicle, Motor, Road, and Environmental Parameters: Fixed Gears: 6,000,8000 RPM Pk Power

Max Motor Power:	$\text{Power}_{\text{max}1} := 185 \cdot \text{kW}$	Fixed Two Gear Ratios:	$\text{GR}_1 := 14.3$ $\text{GR}_2 := 7.4$
Max Motor Torque:	$T_{\text{max}} := 210 \cdot \text{ft} \cdot \text{lbf}$	Battery Energy:	$\text{Energy}_{\text{bat}} := 53 \cdot \text{kW} \cdot \text{hr}$
Power Train 1.5:	$\text{Power}_{\text{max}} := 0.77 \cdot 850 \cdot 370 \cdot \text{W}$		
Max Motor Torque:	$T_{\text{max}} := 280 \cdot \text{ft} \cdot \text{lbf}$	Tire Radius*:	$r_{\text{tire}} := \frac{78.45}{2 \cdot \pi} \cdot \text{in}$
$\text{GR}_{1.5} := 8.2752 \cdot 1.124$			
Max Force, FMaxTire	$\text{Fm}_{\text{tire}1} := \text{GR}_1 \cdot \frac{T_{\text{max}}}{r_{\text{tire}}}$	$\text{Fm}_{\text{tire}2} := \text{GR}_2 \cdot \frac{T_{\text{max}}}{r_{\text{tire}}}$	$\text{Fm}_{\text{tire}1.5} := \text{GR}_{1.5} \cdot \frac{T_{\text{max}}}{r_{\text{tire}}}$
RPM := min ⁻¹			
Max Power, ω :	$\omega_{\text{Pmax}} := \frac{\text{Power}_{\text{max}}}{T_{\text{max}}}$	$\text{RPM}_{\text{Pmax}} := \frac{\omega_{\text{Pmax}}}{2 \cdot \pi}$	$\text{RPM}_{\text{Pmax}} = 6.091 \times 10^3 \text{ RPM}$
Constant Power vehicle velocity, v_{CP} :	$v_{\text{CP}} := \frac{\text{Power}_{\text{max}}}{\text{Fm}_{\text{tire}1.5}}$	$v_{\text{CP}} = 48.653 \text{ mph}$	$\text{Power}_{\text{max}} = 324.749 \text{ hp}$
Time, in seconds:	$t := 0, 0.5 \dots 30$	Lotus Elsie Chassis	$k := 10^3$
Time unit:	$\tau := 1 \cdot \text{sec}$	Curb Weight:	$M_{\text{curb}} := 1350 \cdot \text{kg}$ $M_{\text{curb}} := 2733 \cdot \text{lb}$
Shape Correction Factor:	$\text{SCF} := 0.85$	Average Wind Velocity:	$V_w := 0 \cdot \text{mph}$ $V_{\text{CW}} := 0 \cdot \text{mph}$
Drag Coeff:	$\text{Cd} := 0.3$	Frontal Area*:	$\text{Afg} := 1.127 \cdot \text{m} \cdot 1.7 \cdot \text{m}$
Cross Wind Drag Coff:	$\text{Cd}_{\text{CW}} := 0.000014$	Frontal Area	$\text{Af} := \text{Afg} \cdot \text{SCF}$ $\text{Af} = 1.629 \text{ m}^2$
Air Density:	$\rho := 1.293 \cdot \frac{\text{gm}}{\text{liter}}$	Tire Rolling Resist, Hys:	$\text{RR}_{\text{tire}} := 0.007$ $T_{\text{hys}} := 0 \cdot \frac{\text{sec}}{\text{m}}$
Road Rolling Resist:	$\text{RR}_{\text{road}} := 0.002$	θ (radians):	$\theta := \text{atan}(0.0)$
Passengers2 := 170·lb	$F_{\text{static}} := 1 \cdot \text{N}$	Drive Train Drag Coeff:	Gross Weight: $M_{\text{batt}} := 1000 \text{ lb}$
Rotational Inertia Coeff:	$k_m := 1.08$	$\text{Cdt} := 0.024 \cdot \frac{\text{N}}{\text{mph}^2}$	$M_{\text{gross}} := M_{\text{curb}} + \text{Passengers2}$
			$M_{\text{gross}} = 2.903 \times 10^3 \text{ lb}$

Vehicle Dynamics Equations:

Velocity at Torque Fall:	$v_{\text{T1}} := 6100 \cdot \text{RPM} \cdot 2 \cdot \pi \cdot r_{\text{tire}} \cdot \text{GR}_1^{-1}$	$v_{\text{T1}} = 31.69 \text{ mph}$
Velocity to RPM:	$V_{\text{toR}}(v) := v \cdot (k \cdot 2 \cdot \pi \cdot r_{\text{tire}} \cdot \text{RPM})^{-1}$	$V_{\text{toR}}(61 \cdot \text{mph}) \cdot \text{GR}_2 = 6.076$
Road Resistance, Ft:	$\text{Ft}(v) := [M_{\text{gross}} \cdot g \cdot [T_{\text{hys}} \cdot v \cdot \sin(\theta) + (\text{RR}_{\text{tire}} + \text{RR}_{\text{road}}) \cdot \cos(\theta) + \sin(\theta)]] + F_{\text{static}}$	
Drag Force, Fa:	$\text{Fa}(v) := 0.5 \cdot \rho \cdot \text{Af} \cdot [(v + V_w)^2 \cdot \text{Cd} + \text{Cd}_{\text{CW}} \cdot (V_{\text{CW}})^2] + \text{Cdt} \cdot v^2$	$\omega_{\text{fall}} := 6 \cdot \text{RPM}$
Opposing Force, Fo:	$\text{Fo}(v) := \text{Fa}(v) + \text{Ft}(v)$	$\text{Fo}(60 \cdot \text{mph}) = 430.855 \text{ N}$
Torque/Force Drop Curve:	$T_{\text{fall}}(\omega) := T_{\text{max}} \cdot [1 - (\omega \cdot \text{RPM} - \omega_{\text{fall}}) \cdot ((\omega_{\text{max}} - \omega_{\text{fall}}))^{-1}]$	$\omega_{\text{max}} := 16 \cdot \text{RPM}$
Torque Speed Relation:	$T_m(\omega) := \text{if}(\omega \cdot \text{RPM} \geq \omega_{\text{fall}}, T_{\text{fall}}(\omega), T_{\text{max}})$	
Net Tractive Force:	$\text{Ft}(v) := \text{if}\left(v > 1000 \cdot \text{mph}, \text{GR}_2 \cdot \frac{T_m(V_{\text{toR}}(v) \cdot \text{GR}_2)}{r_{\text{tire}}}, \text{GR}_{1.5} \cdot \frac{T_m(V_{\text{toR}}(v) \cdot \text{GR}_{1.5})}{r_{\text{tire}}}\right)$	
Third Law of Motion: (a is acceleration)	$a(v) := \frac{\text{Ft}(v) - \text{Fo}(v)}{k_m \cdot M_{\text{gross}}}$	$P_m(\omega) := T_m(\omega) \cdot k \cdot 2 \cdot \pi \cdot \omega \cdot \text{RPM}$
	$\text{Power}_{\text{max}} := P_m(8)$	$\text{Power}_{\text{max}} = 344.346 \text{ hp}$

Applying maximum motor torque, find the velocity starting from initial velocity = 0 mph.

End := 20 Given $\frac{d}{dt} v(t) = a(v(t))$ $v(0) = 0$ vel := Odesolve(t, End)

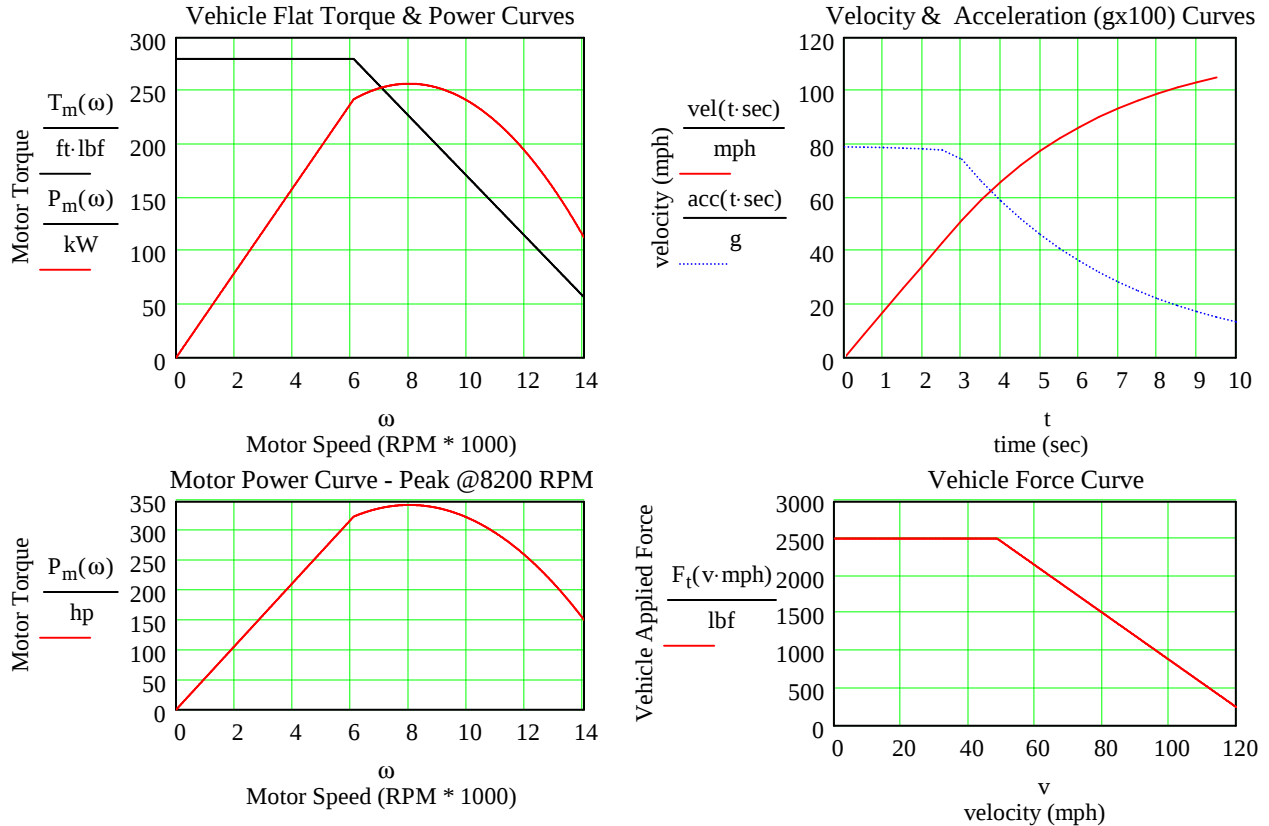
Acceleration in g x 100 acc(t) := a(vel(t·sec))·100 **Roadster Spec is 3.7 sec**

Time := 0·sec time(v) := root(v - vel(Time), Time)

time(60·mph) = 3.551 s

TESLA MOTORS ESTIMATED PERFORMANCE CURVES: Power Train 1.5

Compare with Torque & PowerCurves at: http://www.teslamotors.com/performance/acceleration_and_torque.php



Find the Single Charge (@SOC = 20%) Cruise Range for a given Velocity

Driving Pattern/Profile:

Assume we cruise at constant speed and start, stop, and regen breaking every 15 minutes.

Drive Train Power Efficiency - Battery Loss to Force Commanded Vehicle Velocity:

State of Charge for generator is SOC_{gen} . **SOC_{gen} is 20% for recharge.** 320V HV battery idle power is P_o . 12V battery gives Accessory Power. Gear Efficiencies are modeled dynamically with Drive Train Drag Coefficient C_{dt} . Brake Regen efficiency of kinetic energy is 70%. Then the number of starts per hour as a function of velocity, NS , $NumStarts(v, P_o)$, is

$$\begin{aligned}
 &IPEE := 0.95 \quad \text{Regen} := 0.7 \quad v := 0.2..80 \quad SOC_{gen} := 0.2 \\
 &\text{USABC Round Trip Battery Energy Efficiency} \\
 &RTEff := 0.92 \\
 &Energy_{accel}(v) := Power_{max} \cdot time(v) \\
 &Power_{dissLoss}(v, P_o) := F_o(v) \cdot v + \frac{P_o \cdot watt}{IPEE} \\
 &\underline{NSo \text{ and } NS \text{ are iterative converging estimates of NumStarts}} \\
 &NS_o(v) := 2 \cdot \left(\frac{50 \cdot mph}{v} \right)^2 \quad NS(v, P_o, S) := \frac{Energy_{bat} \cdot (1 - S) - NS_o(v) \cdot \left(Energy_{accel}(v) - \frac{Regen \cdot M_{gross} \cdot v^2}{2} \right)}{Power_{dissLoss}(v, P_o) \cdot 15 \cdot min} \\
 &NumStarts(v, P_o, S) := floor \left[\frac{Energy_{bat} \cdot (1 - S) - NS(v, P_o, S) \cdot \left(Energy_{accel}(v) - \frac{Regen \cdot M_{gross} \cdot v^2}{2} \right)}{Power_{dissLoss}(v, P_o) \cdot 15 \cdot min} \right] \\
 &Cruise_Range(v, P_o, S) := \left[\frac{Energy_{bat} \cdot (1 - S) - NumStarts(v, P_o, S) \cdot \left(Energy_{accel}(v) - \frac{Regen \cdot M_{gross} \cdot v^2}{2} \right)}{Power_{dissLoss}(v, P_o)} \right] \cdot v
 \end{aligned}$$

Single Charge Highway Cruise Range Estimate

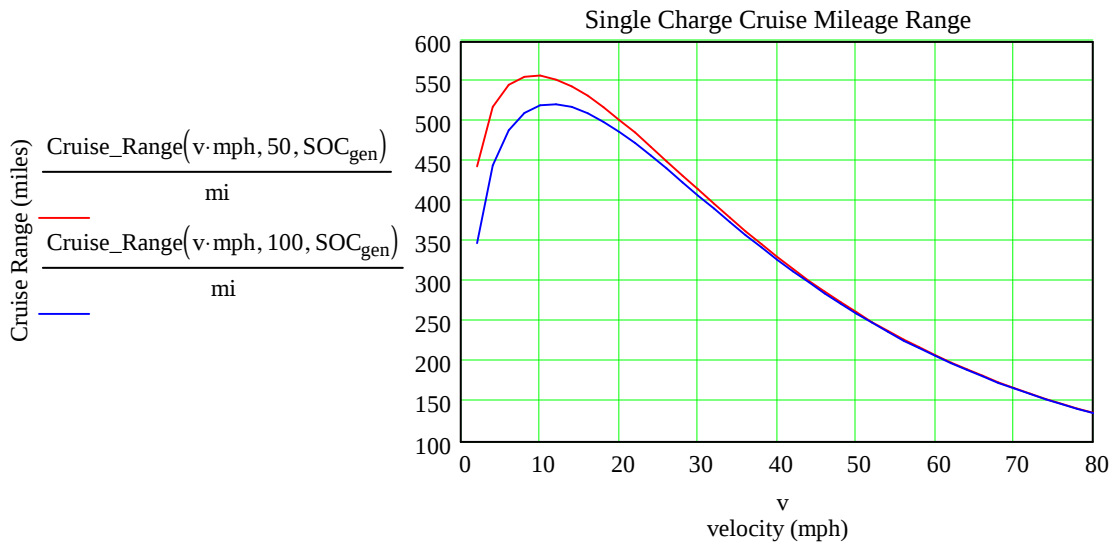
$$\text{Cruise_Range}(30\text{-mph}, 50, \text{SOC}_{\text{gen}}) = 415.439 \text{ mi}$$

$$\text{Cruise_Range}(40\text{-mph}, 50, \text{SOC}_{\text{gen}}) = 331.109 \text{ mi}$$

$$\text{Cruise_Range}(50\text{-mph}, 50, \text{SOC}_{\text{gen}}) = 262.131 \text{ mi}$$

$$\text{Cruise_Range}(60\text{-mph}, 50, \text{SOC}_{\text{gen}}) = 208.307 \text{ mi}$$

$$\text{Cruise_Range}(70\text{-mph}, 50, \text{SOC}_{\text{gen}}) = 167.048 \text{ mi}$$

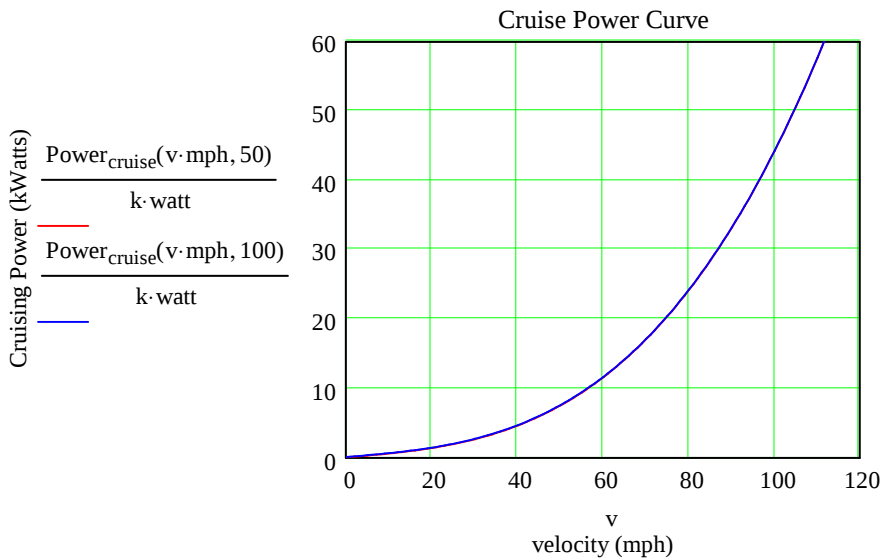


Single Charge "Highway" Cruise Range @70 mph is 150 mph.
Specsmanship: Twice as much range at 30 mph than 70 mph.
Conclusion: I need a bigger or a better battery!

Opposing Force Power Dissipation

$$\text{Power}_{\text{cruise}}(v, P_o) := \text{Power}_{\text{dissLoss}}(v, P_o) \quad v := 0, 1..120$$

$$\text{Power}_{\text{cruise}}(60\text{-mph}, 500) = 1.208 \times 10^4 \text{ watt}$$



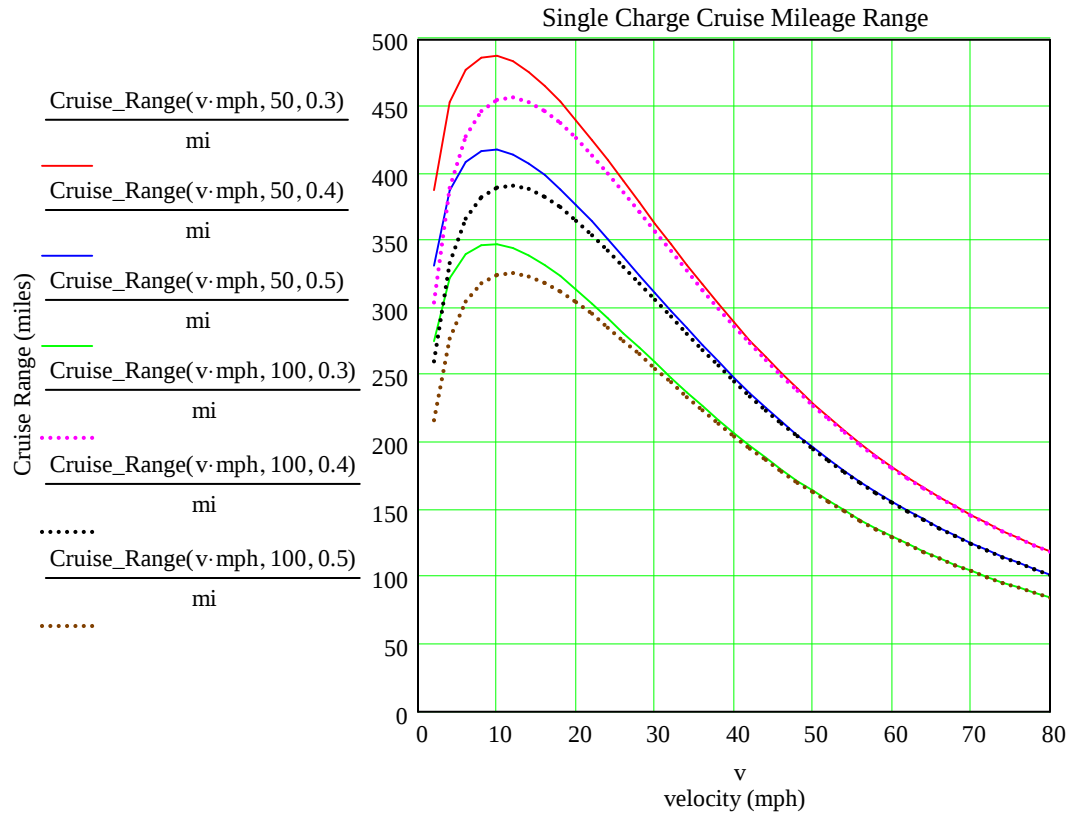
$v := 0, 2..80$

$\text{Cruise_Range}(55\text{-mph}, 100, 0.3) = 203.174 \text{ mi}$

$\text{Cruise_Range}(55\text{-mph}, 100, 0.5) = 145.124 \text{ mi}$

$$\frac{0.5 - 0.25}{0.5} = 0.5$$

$$\frac{\text{Cruise_Range}(55\text{-mph}, 100, 0.25) - \text{Cruise_Range}(55\text{-mph}, 100, 0.5)}{\text{Cruise_Range}(55\text{-mph}, 100, 0.5)} = 0.5$$



FTPF := READPRN("http://www.leapcad.com/Transportation/FedTestProc.TXT")

UDDSF := READPRN("http://www.leapcad.com/Transportation/uddscol.txt")

HWYF := READPRN("http://www.leapcad.com/Transportation/hwycol.txt")

FP10 := READPRN("http://www.leapcad.com/Transportation/FTP10Hz.TXT")

HY10 := READPRN("http://www.leapcad.com/Transportation/HWY10Hz.txt")

US06F := READPRN("http://www.leapcad.com/Transportation/US06PROFILE.TXT")

AER Given Three Different Driving Schedules

Read US06 and FTP Driving Profile Files

<http://www.epa.gov/nvfel/testing/dynamometer.htm>

The US06 cycle represents an 8.01 mile (12.8 km) route with an average speed of 48.4 miles/h (77.9 km/h), maximum speed 80.3 miles/h (129.2 km/h), and a duration of 596 seconds.

The Federal Test Procedure(FTP) is composed of the UDDS followed by the first 505 seconds of the UDDS. It is often called the EPA75. HWY is the Highway schedule.

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t := FTPF<0>    FTP := FTPF<1>    rows(FTP) = 1.875 × 103
UDDS := UDDSF<1>    rows(UDDS) = 1.37 × 103
FP := FP10       HWY := HWYF<1>    rows(HWY) = 766

FTP10 := stack(FP<1>, FP<2>, FP<3>, FP<4>, FP<5>, FP<6>, FP<7>, FP<8>, FP<9>, FP<10>)
time := US06F<0>    US06 := US06F<1>    n := 0..598

FTP10V := submatrix(FP10, 0, rows(FP10) - 1, 1, cols(FP10) - 1)
HWY10V := submatrix(HWY10, 0, rows(HWY10) - 1, 1, cols(HWY10) - 1)

```

Calculate All Electric Range, AER, for Driving Profile File, P, SOC = 20%

```

AER(P) := | Ediss ← 0
          | vold ← 0
          | n ← -1
          | N ← rows(P) - 1
          | while Ediss <  $\frac{\text{Energy}_{\text{bat}}}{\text{kW} \cdot \text{hr}} \cdot (1 - \text{SOC}_{\text{gen}})$ 
          |   | n ← n + 1
          |   | t ← mod(n, N)
          |   | v ← Pt
          |   | vavg ← (v + vold) · 0.5
          |   | Paccel ← km · Mgross · (v - vold) ·  $\frac{\text{mph}}{\text{sec}} \cdot v_{\text{avg}} \text{ mph}$  if v > vold
          |   | Paccel ← km · Mgross · (v - vold) ·  $\frac{\text{mph}}{\text{sec}} \cdot v_{\text{avg}} \text{ mph} \cdot \text{Regen}$  otherwise
          |   | Ediss ← Ediss +  $\frac{(\text{Power}_{\text{dissLoss}}(v \cdot \text{mph}, 100) + P_{\text{accel}}) \cdot \text{sec}}{\text{kW} \cdot \text{hr}}$ 
          |   | vold ← v
          | R ←  $\sum_{m=0}^n \frac{P_{\text{mod}(m, N)} \cdot \text{mph} \cdot \text{sec}}{\text{mi}}$ 

r1 := 0..rows(HWY10) · 10 - 1    HWY10r1 := HWY10Vceil( $\frac{r1+1}{10}$ )-1, mod(r1, 10)

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AER(US06) = 172.598

AER(FTP) = 301.319

AER(FTP10) = 302.511

AER(HWY) = 250.838

$$r1 := 0..rows(HY10) \cdot 10 - 1$$

$$HWY10_{r1} := HWY10V \cdot \left\lceil \frac{r1+1}{10} \right\rceil - 1, \text{mod}(r1, 10)$$

$$AER(FTP) = 301.319$$

$$AER(HWY) = 250.838$$

EPA 20085 Cycle MPG Fuel Economy Least Squares Fit Regression for AER

$$MPG_{city} := \frac{1}{\left(0.003259 + \frac{1.18053}{AER(FTP)}\right)} \quad MPG_{city} = 139.336 \quad MPG_{hwy} := \frac{1}{0.001376 + \frac{1.3466}{AER(HWY)}} \quad X := \frac{1}{40}$$

$$MPG_{epa} := 0.55 \cdot MPG_{city} + 0.45 \cdot MPG_{hwy}$$

$$MPG_{epa} = 143.357$$

$$r := 0..rows(FTP) - 1 \quad Distance_r := \sum_{r=0}^r FTP_r \cdot \frac{10}{60 \cdot 60} \quad max(Distance) = 110.414$$

$$rr := 0..rows(US06) - 1 \quad Distance_{rr} := \sum_{rr=0}^{rr} US06_{rr} \cdot \frac{10}{60 \cdot 60} \quad max(Distance) = 80.08$$

$$WRITEPRN("EFTP.PRN") := AER(FTP) \cdot 40$$

$$E_{FTP} := READPRN("EFTP.PRN")$$

$$max(E_{FTP}) \cdot X = 301.25$$

$$WRITEPRN("EUS06.PRN") := AER(US06) \cdot 40$$

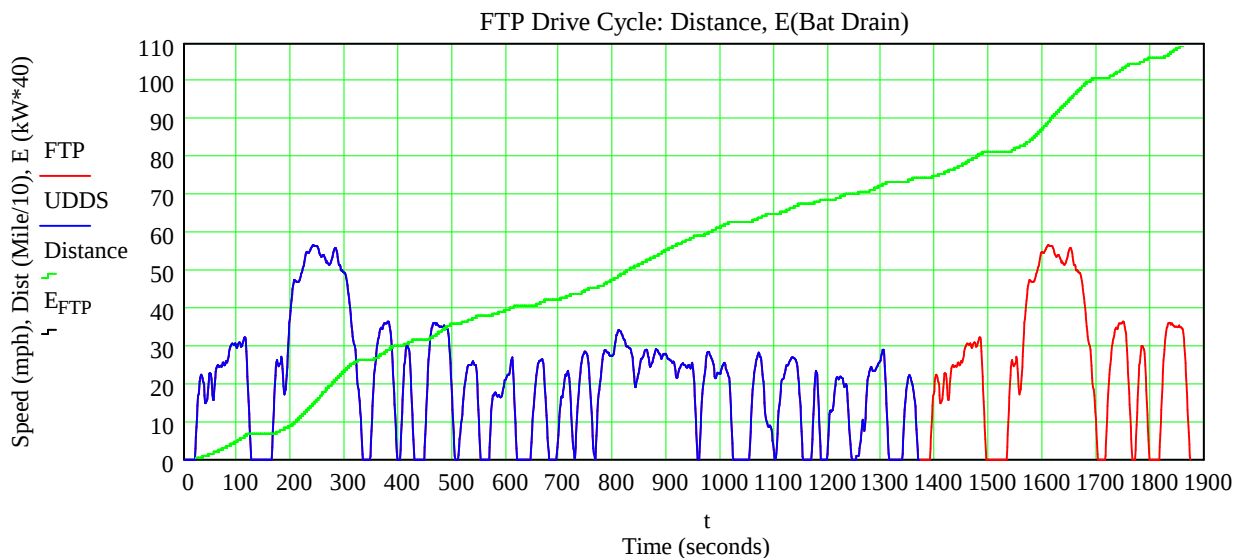
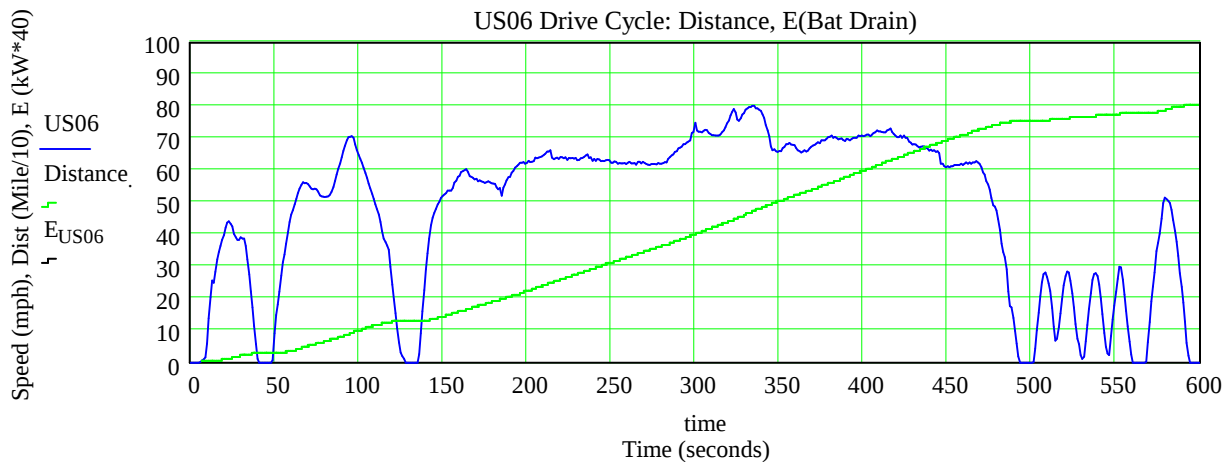
$$E_{US06} := READPRN("EUS06.PRN")$$

$$max(E_{US06}) \cdot X = 172.6$$

$$WRITEPRN("EHWY.PRN") := AER(HWY) \cdot 40$$

$$E_{HWY} := READPRN("EHWY.PRN")$$

$$max(E_{HWY}) \cdot X = 250.75$$



Read Tesla Roadster 1.5 Computer Model Loss Data from File:

Data in Eight Columns:

Speed mph	Total Wh/mi	Ancillary Wh/mi	Tires Wh/mi	Aero Wh/mi	Drivetrain Wh/mi	Range mi	Power kW
$TL := \text{READPRN}("http://www.leapcad.com/Transportation/Tesla\%20Losses.TXT")$							$W \cdot \frac{\text{hr}}{\text{mi}} = 2.237 \text{ N}$
$Speed := TL^{(0)}$	$PwrTesla := TL^{(7)}$	$Speed_{39} = 80$	$Speed_{26} = 54$	$Speed_0 = 2$			
$TV := \left(\frac{Speed \cdot TL^{(1)}}{1000} \right)$	$Tires := \left(\frac{Speed \cdot TL^{(3)}}{1000} \right)$	$Aero := \left(\frac{Speed \cdot TL^{(4)}}{1000} \right)$	$DT := \frac{Speed \cdot TL^{(5)}}{1000}$				
$All := (Tires + Aero + DT)$				$v := 0, 1..100$	$PwrTesla_0 = 0.7$		

Model the Drive Train Losses, DTmodel, as Square of Velocity Assume 300 W of Accessory Power

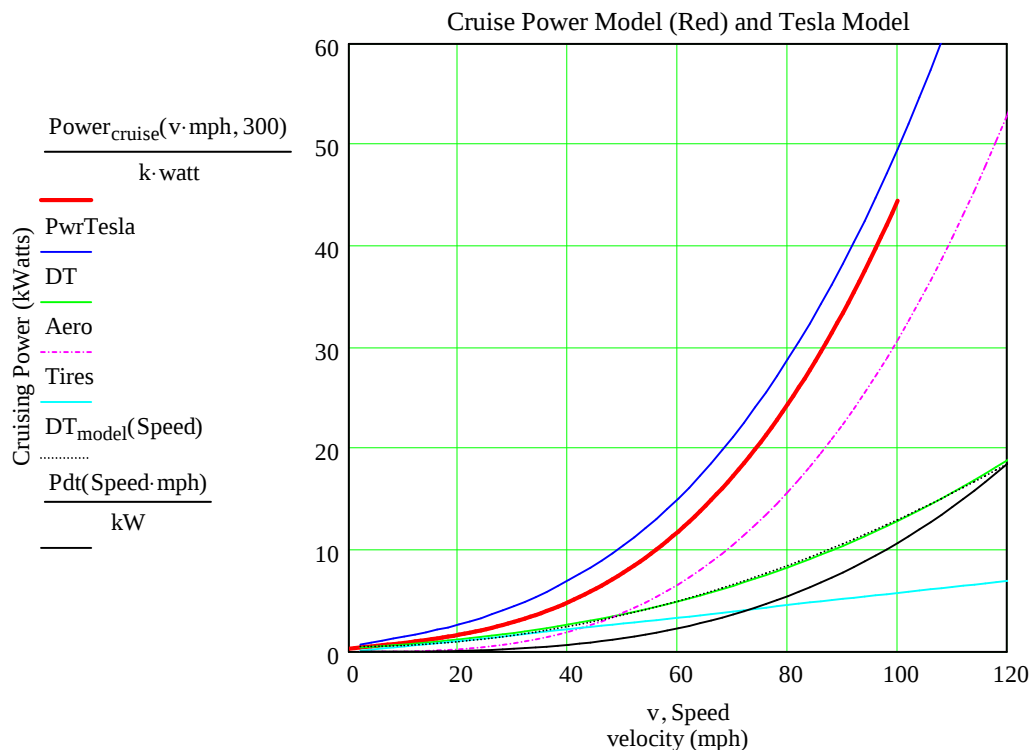
$$guess := \begin{pmatrix} 0.1 \\ 0.001 \end{pmatrix} \quad F(n, a) := \begin{pmatrix} a_0 + a_1 \cdot n^2 \\ n \\ n^2 \end{pmatrix} \quad G := \text{genfit}(Speed, DT, guess, F) \quad G = \begin{pmatrix} 0.501 \\ 1.253 \times 10^{-3} \end{pmatrix}$$

Static Force Term

$$DT_{\text{model}}(v) := G_0 + G_1 \cdot v^2 \quad Pdt(v) := 0.024 \cdot \frac{N}{\text{mph}^2} \cdot v^3$$

$$.5 \cdot \frac{W \cdot \text{hr}}{\text{mi}} = 1.118 \text{ N} \quad G_1 \cdot \frac{W \cdot \text{hr}}{\text{mi} \cdot \text{mph}^2} = 2.804 \times 10^{-3} \frac{N}{\text{mph}^2}$$

$$DT_{\text{mod}} := 0.5 \cdot N + G_1 \cdot \frac{N}{\text{mph}^2} \cdot (60 \cdot \text{mph})^2 \quad DT_{\text{mod}} = 5.012 \text{ N}$$



Find Residual Error Between Cruise Power Force at 54 mph and Tesla's Power
Assign Error to Drive Train Drag Coefficient, Cdt. Cruise Drive Train Drag Force = Cdt * v^2

$$\text{PowerErrorFactor} := \frac{\text{All}_{26} - \frac{\text{Power}_{\text{cruise}}(54 \cdot \text{mph}, 300)}{\text{k-watt}}}{(54)^2}$$

$$\text{Cdt} := \text{PowerErrorFactor} \cdot \frac{1000 \cdot \text{m}}{54 \text{mph} \cdot \text{s}}$$

$$\text{Cdt} = 0.039$$

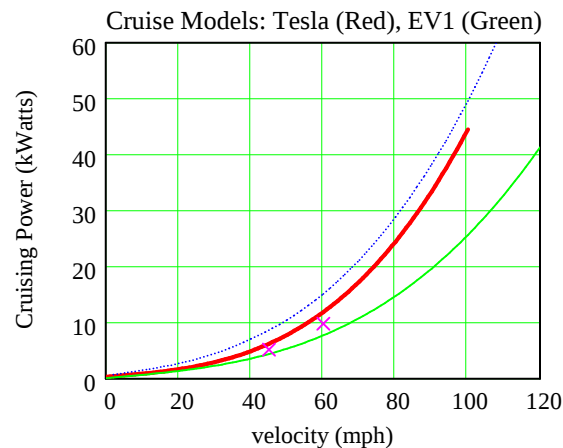
Use this in First Page, Drive Train Coefficient: Cdt = 0.024 @54mph, 0.026 @80,

$$\text{PowerErrorFactor} = 9.515 \times 10^{-4}$$

$$\text{Power Error Factor} = 0.000923$$

Plot EV1 and Tesla Cruise Power Data on same Plot

$$\text{EVDat} := \text{READPRN}(\text{"EV1Cpwr.txt"}) \quad \text{PWR} := \text{EVDat}^{\langle 1 \rangle} \quad \text{Spd} := \begin{pmatrix} 45 \\ 60 \end{pmatrix} \quad \text{Pwr} := \begin{pmatrix} 5.19 \\ 9.79 \end{pmatrix}$$



Petroleum-equivalent efficiency

See also: Electric car: Comparison with internal combustion vehicles (ICEVs)

The Roadster does not actually use gasoline; therefore, petroleum-equivalent efficiency (mpg, l/100 km) cannot be measured directly but instead is calculated using one of several different methods:

A number comparable to the typical Monroney sticker's "pump-to-wheel" fuel efficiency can be calculated based on regulations from the DOE and its energy content for a U.S. gallon of gasoline of 33,705 W·h/gal (also called the Lower Heating Value (LHV) of gasoline)

$$\frac{33705 \frac{\text{W} \cdot \text{h}}{\text{gal}_{\text{ge}}}}{135 \frac{\text{W} \cdot \text{h}}{\text{km}} \times \frac{1.6 \text{ km}}{\text{mi}}} \times 77.6\%_{\text{charging eff.}} = 120 \text{ mpg}_{\text{ge}} = 1.95 \frac{\text{L}_{\text{ge}}}{100 \text{ km}}$$